

NAME _____ INDEX NUMBER _____

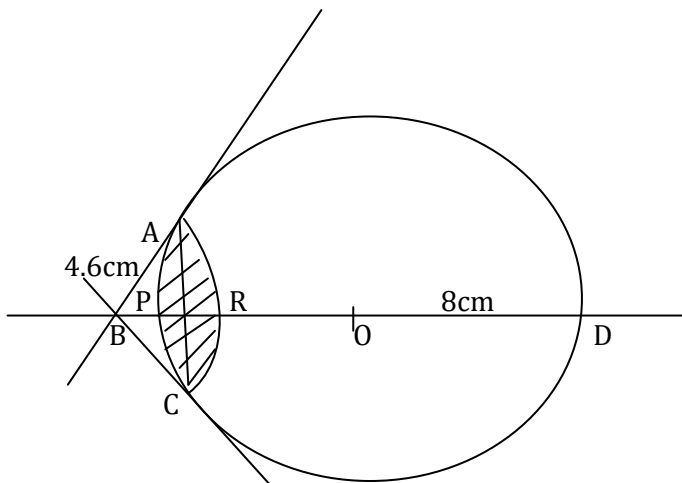
SCHOOL _____ DATE _____

CIRCLES, CHORDS AND TANGENTS

<i>KCSE 1989 – 2012 Form 3 Mathematics</i>	Working Space
<p>1. 1989 Q24 P2</p> <p>The figure below represents the cross section of a metal bar.</p> <div data-bbox="316 535 641 871" data-label="Diagram"></div> <p>The cross section is in the form of a major segment of a circle. M is the midpoint of AB and CM is perpendicular to AB. Given that $AB = CM = 8\text{cm}$. Calculate the area of the cross section (8 marks)</p>	
<p>2. 1990 Q20 P1</p> <p>Two solid spherical balls with centres P and Q touch each other. The balls lie inside and in contact with a hemispherical bowl of centre R. Given that $PQ = 13\text{cm}$, $QR = 16\text{cm}$ and $PR = 19\text{cm}$, calculate the radii of the bowl and the two spherical balls. (8 marks)</p>	

3 **1992 Q8 P2**
 A chord AB of length 13cm subtends an angle of 67° at the circumference of a circle centre O. Find the radius of the circle. (4 marks)

4 **1993 Q24 P1**
 In the figure below O is the centre of a circle whose radius is 8cm. BA and BC are tangents to the circle. PD is a diameter of the circle and AC is a chord of length 8cm. Angle ABC = 120° . ARC is of a circle centre centre B and radius 4.6 cm.



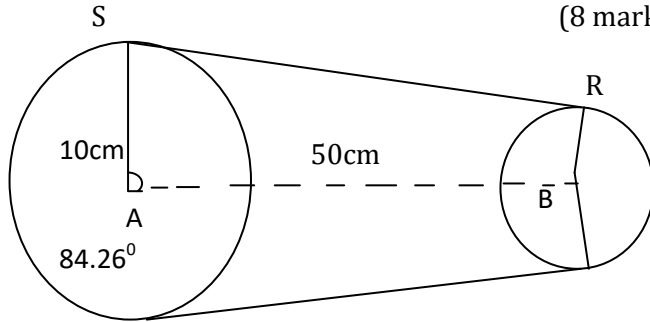
Calculate the area of the shaded region (8 marks)

5. **1994 Q21 P1**

The figure below shows two pulleys with centres A and B and of radii 10cm and 5cm respectively. S and R are contacts points of the belt with the pulleys.

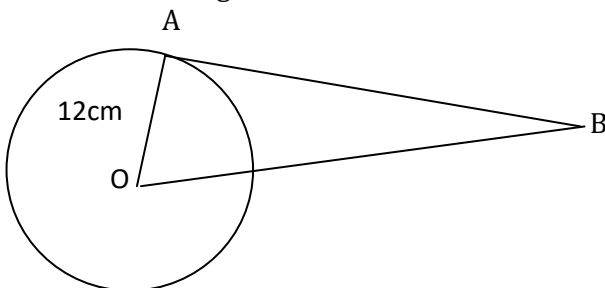
The distance between the centres of the two pulleys is 50cm, and $\angle SAB = 84.26^\circ$. A belt is tied around the two pulleys as shown. Calculate the total length of the belt

(8 marks)



6. **1994 Q11 P2**

In the figure below AB is a tangent to the circle centre O and radius 12cm. The area of the triangle AOB is 120cm^2 . OXB is a straight line.

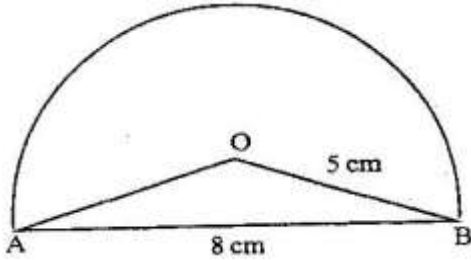


Calculate XB

(4 marks)

7. **1995 Q 19**

(a) In the figure below O is the centre of a circle whose radius is 5 cm. $AB = 8$ cm and $\angle AOB$ is obtuse.

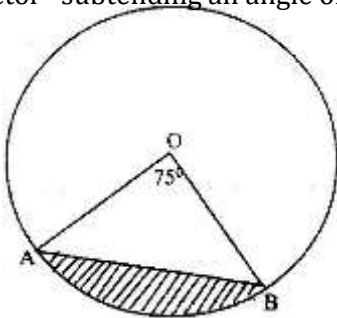


Calculate the area of the major segment (6 marks)

(b) A wheel rotates at 300 revolutions per minute. Calculate the angle in radians through which a point on the wheel turns in one second.

8. **1997 Q 5 P2**

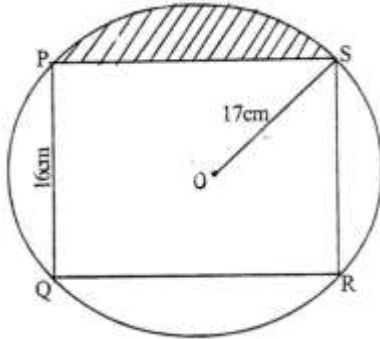
The figure below represents a circle a diameter 28 cm with a sector subtending an angle of 75° at the centre.



Find the area of the shaded segment to 4 significant figures

9 **1998 Q 23 P2**

The figure below represents a rectangle PQRS inscribed in a circle centre O and radius 17cm. $PQ = 16\text{cm}$.

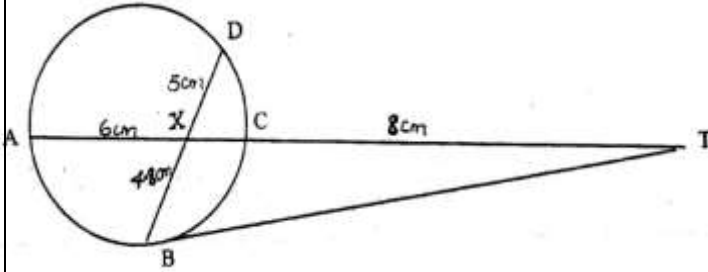


Calculate

- (a) The length PS of the rectangle (2 marks)
- (b) The angle POS (2 marks)
- (c) The area of the shaded region (4 marks)

10 **2000 Q 14 P2**

In the figure below, BT is a tangent to the circle at B.
 AXCT and BXD are straight lines $AX = 6\text{cm}$, $CT = 8\text{cm}$,
 $BX = 4.8\text{cm}$ and $XD = 5\text{cm}$. Find the length of
 (a) XC (b) BT

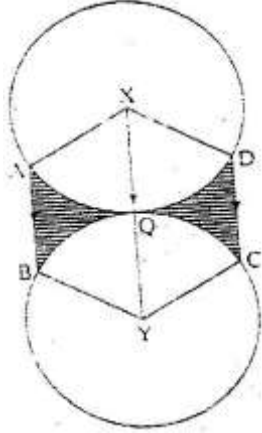
11 **2002 Q 12 P1**

Chords XY and PQ of a circle intersect at a point M
 inside the circle. Given that $MX = 8\text{cm}$, $XY = 14\text{cm}$ and
 $MP = 4\text{cm}$, calculate the length of MQ. (2 marks)

		Working Space
12	<p>2002 Q 23 P1</p> <p>A minor sector of a circle of radius 28cm includes an angle of 135° at the center.</p> <p>a) (i) Convert 135° into radians. Hence of otherwise find the area of the sector.</p> <p>ii) Find the length of the minor arc.</p> <p>b) The sector is folded to form a right circular cone. Calculate the :</p> <p>i) Radius of the cone</p> <p>ii) Height of the cone. (Take the value of π to be $\frac{22}{7}$)</p> <p style="text-align: right;">(8 marks)</p>	

13 **2003 Q 19 P1**

The figure below shows two circles each of radius 7 cm, with centers at X and Y. The circles touch each other at point Q.



Given that $\angle AXD = \angle BYC = 120^\circ$ and lines AB, XQY and DC are parallel, Calculate the area of:

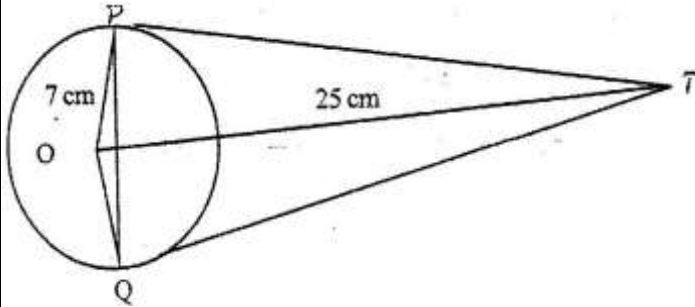
- Minor sector XAQD (Take $\pi^{22/7}$)
- The shaded regions.

(8 marks)

14

2004 Q 14 P1

The figure below shows a circle, centre, O of radius 7cm. TP and TQ are tangents to the circle at points P and Q respectively. OT = 25cm.



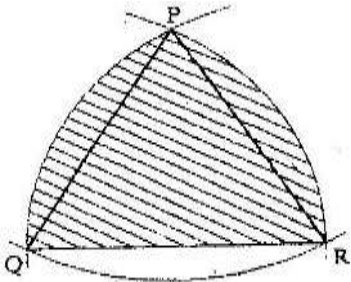
Calculate the length of the chord PQ (3 marks)

15

2005 Q 6 P1

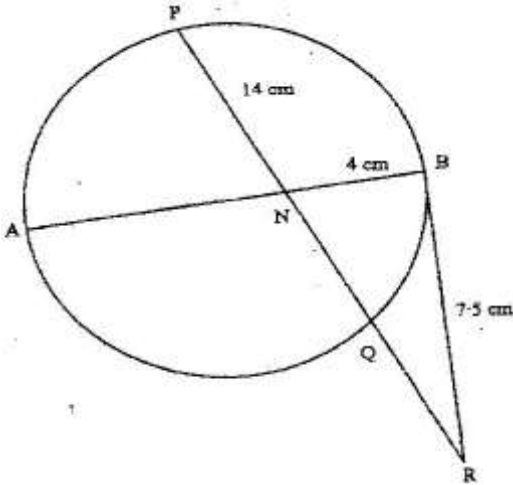
A point R divides a line PQ internally in the ratio 3:4. Another point S, divides the line PR externally in the ratio 5:2. Given that PQ = 8cm, calculate the length of RS, correct to 2 decimal places. (3 marks)

16 **2007 Q 14 P1**
 In the figure below, PQR is an equilateral triangle of side 6 cm. Arcs QR, PR and PQ arcs of circles with centers at P, Q and R respectively.



Calculate the area of the shaded region to 4 significant figures (4 marks)

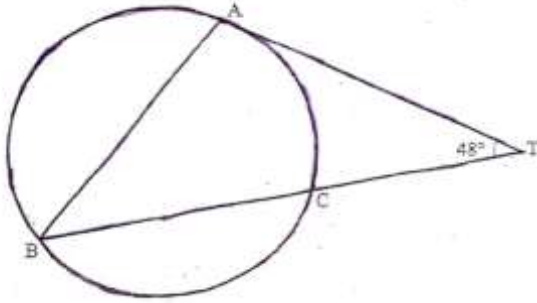
17 **2007 Q 11 P2**
 In the figure below AB is a diameter of the circle. Chord PQ intersects AB at N. A tangent to the circle at B meets PQ produced at R.



Given that $PN = 14\text{cm}$, $NB = 4\text{ cm}$ and $BR = 7.5\text{ cm}$, calculate the length of:
 (a) NR (1 mark)
 (b) AN (3 marks)

18 **2009 Q 15 P2**

In the figure below, AT is a tangent to the circle at A.
 Angle ATB = 48° , BC = 5cm and CT = 4cm

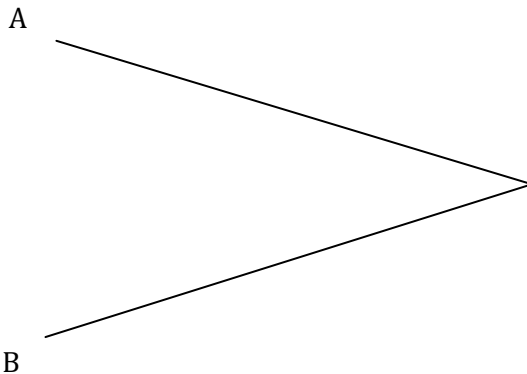


Calculate the length of AT (2 marks)

19 **2011 Q 10 P2**

(a) In the figure below, lines NA and NB represent tangents to a circle at points A and B. Use a pair of compasses and ruler only to construct the circle.

(2 marks)

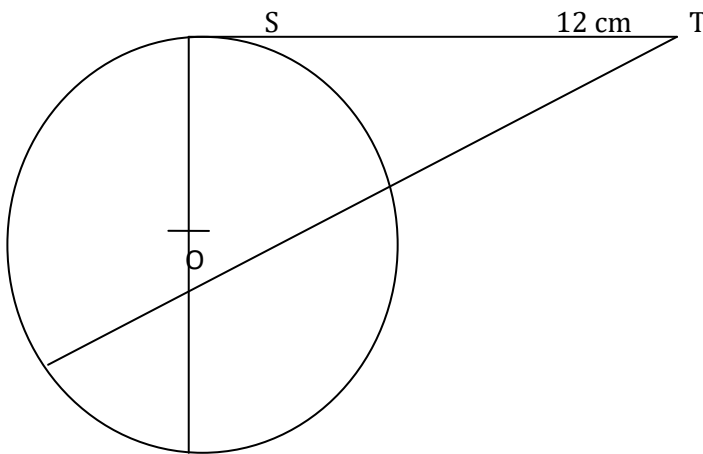


(b) Measure the radius of the circle. (1 mark)

20 **2012 Q14 P2**

In the figure below, the tangent ST meets chord VU produced at T . Chord SW passes through the centre, O , of the circle and intersects chord VU at X . Line

$ST = 12\text{cm}$ and $UT = 8\text{cm}$.



- (a) Calculate the length of chord VU . (2 marks)
(b) If $WX = 3\text{cm}$ and $VX: XU = 2:3$, find SX . (2 marks)