

CIRCLES, CHORDS AND TANGENTS MARKING SCHEME

1.	67.35cm^2 <p style="text-align: right;">1989Q24</p>	8M	
2.	$r^1 = 5\text{cm}$ $r^2 = 5\text{cm}$ r^3 $= 24\text{cm}$ <p style="text-align: right;">1990Q20</p>	8M	
3.	$2r = \frac{a}{\sin A}$ $2R = \frac{13}{\sin 67}$ $2r = 14.122$ $r = 7.061\text{cm}$ <p style="text-align: right;">1992Q8</p>	4M	$360^\circ - 168.520 = 191.48^\circ$ $\frac{191.48}{360} \times 3.142 \times 20$ $= 33.42\text{cm}$ $= 49.75 + 14.71 + 33.42$ $= 147.6\text{cm}$ <p style="text-align: right;">1994Q21</p>
4.	<p>Area of sector ABC $= \frac{120}{360} \times 3.142 \times 4.62$ $= 22.16\text{cm}^2$</p> <p>Area of triangle ABC $= \frac{1}{2} \times 4.6 \times 4.6 \sin 120^\circ$ $= 9.16\text{cm}^2$</p> <p>Area of section $= 22.16 - 9.16$ $= 13\text{cm}^2$</p> <p>Area of sector AOC $= \frac{60}{360} \times 3.142 \times 8 \times 8$ $= 33.51\text{cm}^2$</p> <p>area of triangle AOC $= \frac{1}{2} \times 8 \times 8 \sin 60^\circ$ $= 27.71\text{cm}^2$</p> <p>Area of section $= 33.51 - 27.71$ $= 5.8\text{cm}^2$</p> <p>Area of shaded region $= 5.8 + 13$ $= 18.8\text{cm}^2$ 18.803cm^3</p> <p style="text-align: right;">1993Q24</p>	8M	<p>6.</p> <p>$A = \frac{1}{2}bxh$ $120 = \frac{1}{2} \times 12 \times h$ $120 = 6h$ $h = 20\text{cm}$ $12^2 + 20^2 = 544$ $\sqrt{544} = 23.32\text{cm}$ $xb = 11.32\text{cm}$</p> <p style="text-align: right;">1994Q11</p>
5.	$\sin 84.26 = \frac{x}{50}$ $x = 50 \sin 84.26$ $= 49.75\text{cm}$ $84.26 \times 2 = 168.52^\circ$ $\frac{168.52}{360} \times 3.142 \times 10$ $= 14.71\text{cm}$	8M	<p>7.</p> <p>a) $b^2 = a^2 + c^2 - 2ac \cos B$ $8^2 = 5^2 + 5^2 - 2 \times 5 \times 5 \cos B$ $64 = 25 + 25 - 50 \cos B$ $50 \cos B = 50 - 64$ $50 \cos B = -14$ $\cos B = \frac{-14}{50} = -0.28$ $B = 106.26^\circ$ $3600 - 106.260 = 253.740$</p> <p>Area of sector AOB = $\frac{253.74}{360} \times 3.142 \times 5^2$ $= 55.36\text{cm}^2$</p> <p>Area of triangle AOB $= \frac{1}{2} \times 5 \times 5 \sin 106.26$ $= 12\text{cm}^2$ $= 55.36 + 12$ $= 67.36\text{cm}^2$</p> <p style="text-align: right;">1995Q19</p>
8.	<p>Area of the sector $= \frac{75^\circ}{360} \times \frac{22}{7} \times 14 \times 14$ $= 128.3\text{cm}^2$</p> <p>Area of Δ $= \frac{1}{2} \times 14 \times 14 \sin 75^\circ$ $= \frac{1}{2} \times 14 \times 14 \times 0.9659$ $= (6,5)$ $= 94.64\text{cm}^2$</p> <p>Area of segment = $128 - 94.64$</p>	4M	<p>M1</p> <p>M1</p> <p>M1</p> <p>A1</p> <p>4 M</p>

	= 33.66 Or (33.68)LM	
	1997Q5	
9.	(a) ps = $(34^2 - 16^2) = 900$ = 30 (b) cos Pos $= \frac{17^2 + 17^2 - 30^2}{2 \times 17 \times 17} = \frac{-322}{578}$ = -0.5572 Cos Pos = $123^{050} (2)$ (123.86) (c) Area of sector $= \frac{123.8}{360} \times 3.142 \times 17 \times 17$ = 312.3 Area of Δ $= \frac{1}{2} \times 17 \times 17 \sin 123^{050}$ $= \frac{1}{2} \times 17 \times 17 \times 0.8307$ = 120 Area of segment = $312.3 - 120 = 192.3$	M1 M1 A1 M1 M1 A1 8M
	1998Q23	
10.	a) $6 \cdot xc = 4.8 \times 5$ $xc = \frac{4.8 \times 5}{6} = 4$ b) $BT^2 = 6 + 4 + 8) \times 8$ $= 18 \times 8 = 144$ BT = 12	M1 A1 M1 A1
	2000Q14	
11.	MY = 14.8 = 6cm Therefore 4 (MQ) = 8 x 6 MQ = 12	M1 A1 2 M
	2002Q12	
12.	a). i). $135 \times \frac{\pi}{180} \times \frac{3\pi}{4}$ Area of sector $= \frac{3}{8} \times 2^2 \times 282$ = 924cm ² ii). Length of mirror $\frac{3}{8} \times 2^2 \times 28 \times 2 = 66\text{cm}$ b). i). $r\pi l = \text{area of curved surface}$ $r\pi l = \frac{924 \times 7}{22 \times 28}$ = 10.5m $H = \sqrt{28^2 - 10.5^2}$	B1 M1 A1 B1 A1 B1 B1 8 M

	= 25.96	
	2002Q23	
13.	a). Area = $\frac{120}{360} \times 7 \times 7 \times \frac{22}{7}$ = $5^{11/3} \text{cm}^2$ b). $\frac{1}{2} AD = 7 \sin 60^0$ $\frac{7\sqrt{3}}{2} = 6.062$ AB = $14.2 \times 7 \cos 60^0$ = $14.2 \times 7 \times 0.5$ Area of trapezium XABY = $\frac{1}{2} (7+14) \times 6.062$ = 63.65cm ² c). Area of shaded region = $2(63.65 - 5^{11/3})$ = $127.30 - 102.67$ = 24.63cm ²	M1 A1 M1 M1 M1 A1 M1 A1 8 M
	2003Q19	
14	Area of equilateral = $\frac{1}{2} \times 5 \times 5 \sin 60^0$ = $\frac{1}{2} \times 5 \times 5 \times 0.866$ = 10.825cm ² = 64.95cm volume of the prism = 64.95 x 20 1299cm ³	B1 B1 B1 M1 M1
		M1 M1 A1 8 M
	2004Q14	
15.		B1

	$\overrightarrow{PR} = \frac{3}{7} PQ$ $\overrightarrow{PR} = \frac{3}{5} PS$ But $\overrightarrow{PR} = \overrightarrow{PR}$ $\frac{3}{7} PQ = \frac{3}{5} PS$	1 M 1 M A1	2005Q6
16.	Area of each sector $\frac{60}{360} \times \pi \times 6^2$ 18.84955592cm^2 Area of Δ $= \frac{1}{2} \times 6 \times 6 \times \sin 60$ $= 15.58845727 \text{cm}^2$ Therefore area of shaded region $18.84955592 + 2$ $(18.84955592 - 15.58845727)$ $18.84955592 + 6.522197303$ 22.11065457 22.11cm^2	M1 A1 A1 M1 4 m	2007Q14
17.	$N = \sqrt{42} + 7.52$ $= 8.5$ $QR = (14 + 8.5) = 7.52$ $Qr = 25$ $4x \text{ an} = 14x(8.5 - 2.5)$ $AN = \frac{14 \times 5}{4}$ $= 12 \text{cm}$	B1 M1 M1 M1 A1 4 M	2007Q11
18.	$AT^2 = 9 \times 4$ $= 36$ $AT = 6 \text{cm}$	M1 A1 2 M	2009Q15
19.	$R = 2.5 \pm 0.1 \text{ cm}$	B1 B1 A1 3m	2011Q10

20.	(a) Let UV be x cm. $VT \times UT = ST^2$ $(x + 8)8 = 12^2$ $8x = 144 - 64$ $= 80$ $x = 10 \text{cm}$ (b) $VX = \frac{2}{5} \times 10 = 4 \text{ cm}$ $XU = 10 - 4 \text{ cm}$ $= 6 \text{ cm}$ $= VX \times XU$ or $SX = \sqrt{14^2 - 12^2}$ $= SX \times 3 = 4 \times 6$ $SX = 7.211$ $SX = 8 \text{cm}$ Accept 7.2	M1 A1 M1 A1 4	2012 Q14 P2
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