

APPROXIMATIONS AND ERRORS MARKING SCHEME

1.	$R = 8.5$ $r = 5.5$ $v = \pi R^2 h - \pi r^2 h$ $= \frac{22}{7} \times 14 (8.5 - 5.5) (8.5 + 5.5)$ $= 44 (3) (14)$ $= 1848 \text{cm}^3$ <p style="text-align: right;">1996Q15</p>	B1 M1 A1 3M		<p>Indicated perimeter $2(18 + 12) = 60 \text{cm}$</p> <p>Absolute error = $\frac{62 - 58}{2} = 2$</p> <p style="margin-left: 40px;">$= \frac{2}{60} \times 100$</p> <p style="margin-left: 40px;">$= 3.1\%$ avoid $\frac{10\%}{3}$</p> <p style="text-align: right;">2000Q10</p>
2.	<p>a). $R \frac{1}{0.00001} = \frac{1}{1.6} \times 10^5$ $= 62500$</p> <p>b). Appropriate value $\frac{1}{0.00315 - 0.00313}$ $= \frac{1}{0.00002}$ $= \frac{1}{2} \times 10^5$ $= 50000$</p> <p>ii). Error = $62500 - 50000$ $= 12500$</p> <p style="text-align: right;">1997Q16</p>	A1 M1 A1 B1 3 M	6.	<p>Absolute error = $0.5 + 0.5 + 0.5 = 1.5$ % error = $\frac{1.5}{33} \times 100\%$ $= 4.55\%$ (to 2d.p) $= 4.54\%$ (if Logs used)</p> <p style="text-align: right;">2002Q8</p>
3.	<p>a) $c = 2 \times 2.8 \times \frac{22}{7} = 17.6 \text{cm}$ $= \frac{c}{\pi} = 17.6 \times \frac{7}{22} = 5.6$</p> <p>b) $3.142 \times 2.8 \times 2 = 17.595$ $3.142 \times 5.5 = 17.281$ $3.142 \times 5.7 = 19.909$ Limits : $17.28 + 17.91$</p> <p style="text-align: right;">1998Q15</p>	M1 M1 A1 2M	7.	<p>L.U = 1cm A.E = 0.5 Limits of A are 3.5 and 4.5 Limits of 6 are 5.5. and 6.5 Min Area = $\frac{1}{2} \times 3.5 \times 5.5$ $= 9.625$</p> <p>Maximum area = $\frac{1}{2} \times 4 \times 6$ $= 14.625$</p> <p>Working area = $\frac{1}{2} \times 4 \times 6$ $= 12.000$</p> <p>Workign area - Minimum area $= 12 - 9.625$ $= 2.375$</p> <p>Max area - Working area $= 14.625 - 12 = 2.625$</p> <p>Absolute error in area $= \frac{2.375 + 2.625}{2} = 2.5$</p> <p>b). % Error = $\frac{\text{A.E}}{\text{A.M}} \times 100$ $= \frac{2.5}{12} \times 100 = 20 \frac{5}{6} \%$</p> <p style="text-align: right;">2005Q9</p>
4.	<p>a). Maximum possible area $4.11 \times 2.21 = 9.083 \text{m}^2$</p> <p>Minimum possible area $4.09 \times 2.19 = 8.9571 \text{m}^2$</p> <p>b). Maximum possible wastage $9.0831 - 8.9571 = 0.126 \text{m}^2$</p> <p style="text-align: right;">1999Q9</p>	M1 A1 B1 3 M	8.	<p>$800 \times 0.006 = 4.8$</p>
5.	<p>Maximum perimeter $2(18.5 + 12.5) = 62 \text{cm}$</p> <p>Minimum perimeter $2(17.5 + 11.5) = 58 \text{cm}$</p>			

	$\% \text{ error} = \frac{4.8 - (788 \times 0.006) \times 100\%}{788 \times 0.006}$ $= \frac{0.072}{4.728} \times 100\%$ $= 1.523\%$ <p style="text-align: right;">2006Q4</p>	M1 A1 3m
9.	<p>Greatest possible error</p> $= \frac{64(3.15-3.05)}{2}$ $= \frac{201.6 - 195.2}{2}$ $= 3.2\text{cm}^2$ <p style="text-align: right;">2007Q8</p>	M1 A1 2m
10.	$0.05 \times 6 = 0.3$ $\% \text{ error} = \frac{0.3}{50 \times 6} \times 100$ $= 0.1\%$ <p style="text-align: right;">2008Q5</p>	M1 M1 A1 3m
11.	$\frac{(7.55 \times 5.25) - (7.45 \times 5.15)}{2}$ $\frac{0.635}{7.5 \times 5.2} \times 100\%$ $\left(\frac{0.05}{7.5} + \frac{0.05}{5.2}\right) \times 100$ $= 1.628\%$ <p style="text-align: right;">2010Q1</p>	M1 M1 A1 3
12.	$\text{Max}_A = 4\pi(7.5)^2$ $4 \text{Max}_A = 4\pi(6.5)^2$ <p>Absolute error = $\frac{4\pi(7.5^2 - 6.5^2)}{2}$</p> $\% \text{ Error} = \frac{28\pi}{4\pi \times 7^2} \times 100\%$ $= 14.29\%$ <p style="text-align: right;">2011Q9</p>	M1 M1 M1 A1 4

13.	<p>Minimum possible area.</p> $= \frac{1}{2}(6.35 \times 3.45)$ $= 10.95375 \text{ cm}^2$ <p>Maximum possible area</p> $= \frac{1}{2} \times 6.45 \times 3.55$ $= 11.44875 \text{ cm}^2$ <p>Maximum absolute error in area</p> $= \frac{11.44875 - 10.95375}{2}$ $= 0.2475 \text{ cm}^2$ <p style="text-align: right;">2012 Q11 P2</p>	M1 M1 A1 3
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